## Source transformations

Consider the two circuits below. In particular, look at the current and voltage of  $R_L$  in each circuit. Using any of the techniques we seen so far, it is easy to find  $i_{RL}$  and  $v_{RL}$  for each case.



 $i_{RL} = 1.67 \text{ mA}, P = 2.78 \text{ mW}$ 

 $v_{RL} = 1.67 \text{ V}, P = 2.78 \text{ mW}$ 

Interesting: From the point of view of the resistor  $R_L$ , the series combination of the voltage source and resistor  $R_S$  gives the exact same result as the parallel combination of current source and resistor  $R_P$ .

The series combination seems to behave *identically* to the parallel combination. This suggests that we may, in the right circumstances, replace one configuration for the other. Making this switch is known as a *source transformation*.



These are perfectly viable substitutions. From the point of view of whatever circuitry is attached to the two terminals, the result will be exactly the same for the two source configurations.

If you are trying calculate something about the two components ( $V_S$ - $R_S$  or  $I_P$ - $R_P$ ), you cannot transform them. In transforming them, you lose the ability to calculate a specific property.

This is an example of bigger, more important idea known as the Thevenin equivalent of circuit. We will introduce this later, and make extensive use of it in discussing amplifiers, etc.



Use a source transformation to put everything in parallel.

 $I_S = V_S/R_1 = 50 \text{ V}/25 \Omega = 2\text{A}.$ <sup>2</sup>

Then use a current divider:

$$i_{R4} = \frac{\frac{1}{R_4}}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4}} I_S$$
  
=  $\frac{\frac{1}{100 \Omega}}{\frac{1}{25 \Omega} + \frac{1}{50 \Omega} + \frac{1}{200 \Omega} + \frac{1}{100 \Omega}} (2 \text{ A}) = 0.267 \text{ A}$  Easy.

 $l_{R4}$ 



## **Example 3** (An incorrect application)



The previous example worked nicely so use the same method. Transform  $V_s \& R_1$ , and use current divider with the total current.



It seems nice, but it is wrong because you cannot transform the component for which you are trying to find voltage or current. (To see that it is wrong, insert  $i_{R1} = 27.5$  mA in the original circuit and show that there are serious inconsistencies with the currents and voltages.)

## **Example 3** (Redo it correctly.)



Find  $i_{R1}$  in the circuit at left.

Transform  $I_S \& R_2$ .





Transform two voltage sources to current sources. (Pay attention to polarity.)



## Example 4 (cont.)

Add the parallel current sources into one. Combine the parallel resistors into one.



 $I_{eq} = 6A - 12A + 36A = 30A.$ 

 $R_{eq} = 20 \ \Omega || 5 \ \Omega || 6 \ \Omega = 2.4 \ \Omega.$ 

Transform *I*<sub>eq</sub> & *R*<sub>eq</sub>:

Use voltage divider:

